Division at Ravensbury

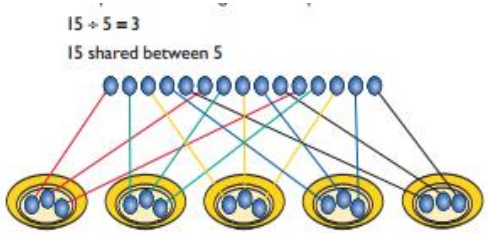
Year 1

Children must have secure counting skills- being able to confidently count in 2s, 5s and 10s.
Children should be given opportunities to reason about what they notice in number patterns.

Group AND **share small quantities- understanding the difference between the two concepts.**

Sharing

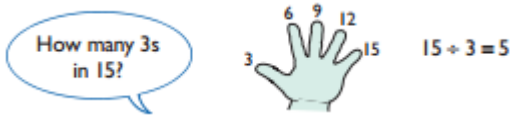
Develops importance of one-to-one correspondence.



Children should be taught to share using concrete apparatus.

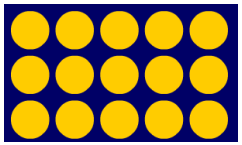
Grouping

Children should apply their counting skills to develop some understanding of grouping.



Use of arrays as a pictorial representation for division.

15 ÷ 3 = 5 There are 5 groups of 3.



Year 2

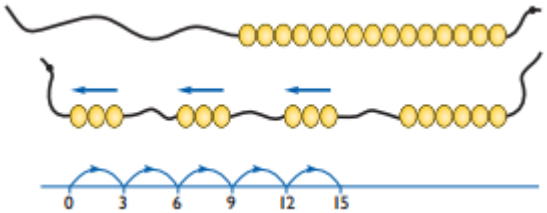
÷ = signs and missing numbers

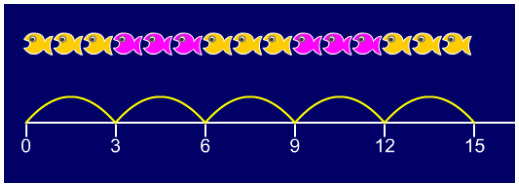
6 ÷ 2 = □ □ = 6 ÷ 2
6 ÷ □ = 3 3 = 6 ÷ □
□ ÷ 2 = 3 3 = □ ÷ 2
□ ÷ ∇ = 3 3 = □ ÷ ∇

Know and understand sharing and grouping- introducing children to the ÷ sign.
Children should continue to use grouping and sharing for division using practical apparatus, arrays and pictorial representations.

Grouping using a numberline

Group from zero in jumps of the divisor to find our 'how many groups of 3 are there in 15?'.
15 ÷ 3 = 5





Continue work on arrays. Support children to understand how multiplication and division are inverse. Look at an array – what do you see?

Mental methods:

Children should count regularly, on and back, in steps of 2, 3, 5 and 10.

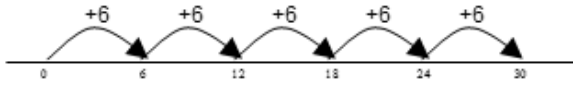
Year 3

÷ = signs and missing numbers

Continue using a range of equations as in year 2 but with appropriate numbers.

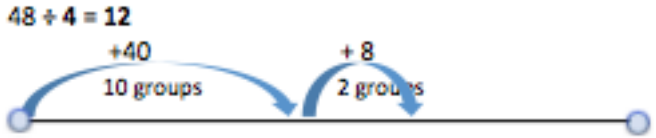
Grouping

How many 6's are in 30?
30 ÷ 6 can be modelled as:

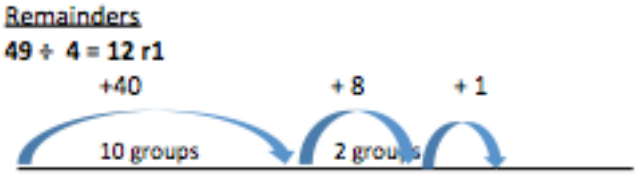


Becoming more efficient using a numberline

Children need to be able to partition the dividend in different ways.



Remainders

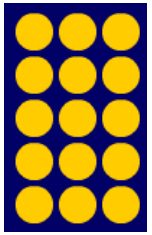


Sharing – 49 shared between 4. How many left over?

Grouping – How many 4s make 49. How many are left over?

Place value counters can be used to support children apply their knowledge of grouping.
For example:
60 ÷ 10 = How many groups of 10 in 60?
600 ÷ 100 = How many groups of 100 in 600?

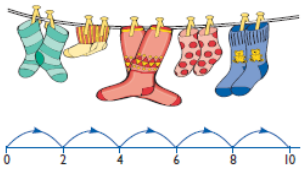
15 ÷ 5 = 3 There are 3 groups of 5.



Mental methods

Children should experience regular counting on and back from different numbers in 1s and in multiples of 2, 5 and 10.

They should begin to recognise the number of groups counted to support understanding of relationship between multiplication and division.



2 + 2 + 2 + 2 + 2 = 10
2 × 5 = 10
2 multiplied by 5
5 pairs
5 hops of 2

Children should begin to understand division as both sharing and grouping.

Sharing – 6 sweets are shared between 2 people. How many do they have each?

Grouping-
How many 2's are in 6?

They should use objects to group and share amounts to develop understanding of division in a practical sense.
E.g. using Numicon to find out how many 5's are in 30?
How many pairs of gloves if you have 12 gloves?

Children who are able to count in twos, threes, fives and tens can use this knowledge to work out other facts such as 2 × 6, 5 × 4, 10 × 9. Show the children how to hold out their fingers and count, touching each finger in turn. So for 2 × 6 (six twos), hold up 6 fingers:

Touching the fingers in turn is a means of keeping track of how far the children have gone in creating a sequence of numbers. The physical action can later be visualised without any actual movement.

This can then be used to support finding out 'How many 3's are in 18?' and children count along fingers in 3's therefore making link between multiplication and division.

Children should continue to develop understanding of division as sharing **and** grouping.

Children should be given opportunities to find a half, a quarter and a third of shapes, objects, numbers and quantities. Finding a fraction of a number of objects to be related to sharing.

They will explore visually and understand how some fractions are equivalent – e.g. two quarters is the same as one half.

Use children's intuition to support understanding of fractions as an answer to a sharing problem.

3 apples shared between 4 people = $\frac{3}{4}$

Noticing how counting in multiples if 2, 5 and 10 relates to the number of groups you have counted (introducing times tables)

An understanding of the more you share between, the less each person will get (e.g. would you prefer to share these grapes between 2 people or 3 people? Why?)

Mental Methods:

Children should count regularly, on and back, in steps of 3, 4 and 8. Children are encouraged to use what they know about known times table facts to work out other times tables. This then helps them to make new connections (e.g. through doubling they make connections between the 2, 4 and 8 times tables).

Children will make use multiplication and division facts they know to make links with other facts.
3 x 2 = 6, 6 ÷ 3 = 2, 2 = 6 ÷ 3
30 x 2 = 60, 60 ÷ 3 = 20, 2 = 60 ÷ 30

They should be given opportunities to solve grouping and sharing problems practically (including where there is a remainder but the answer needs to given as a whole number)
e.g. Pencils are sold in packs of 10. How many packs will I need to buy for 24 children?

Children should be given the opportunity to further develop understanding of division (sharing) to be used to find a fraction of a quantity or measure.

Use children's intuition to support understanding of fractions as an answer to a sharing problem.

3 apples shared between 4 people = $\frac{3}{4}$

Vocabulary

inverse

See Y1 and Y2

Inverses and related facts – develop fluency in finding related multiplication and division facts.

Develop the knowledge that the inverse relationship can be used as a checking method.

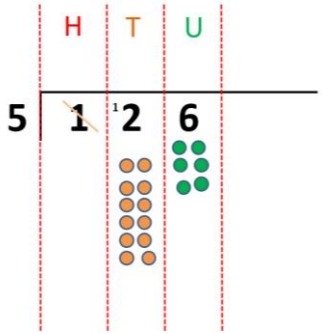
Questions for Mastery and Reasoning

Questions in the context of money and measures that involve remainders (e.g. How many lengths of 10cm can I cut from

Children should begin to explore finding simple fractions of objects, numbers and quantities. E.g.*16 children went to the park at the weekend. Half that number went swimming. How many children went swimming?* **Vocabulary** share, share equally, one each, two each…, group, groups of, lots of, array **Questions for Mastery and Reasoning** How many groups of…? How many in each group? Share… equally into… What can do you notice? True or false? I can only halve even numbers. *Grouping and sharing are different types of problems. Some problems need solving by grouping and some by sharing. Encourage children to practically work out which they are doing.*	Secure understanding of grouping means you count the number of groups you have made. Whereas sharing means you count the number of objects in each group. **Vocabulary** group in pairs, 3s … 10s etc equal groups of divide, ÷, divided by, divided into, remainder **Questions for Mastery and Reasoning** How many 10s can you subtract from 60? I think of a number and double it. My answer is 8. What was my number? If 12 x 2 = 24, what is 24 ÷ 2? Questions in the context of money and measures (e.g. how many 10p coins do I need to have 60p? How many 100ml cups will I need to reach 600ml?)	81cm of string? You have £54. How many £10 teddies can you buy?) What is the missing number? 17 = 5 x 3 + __ __ = 2 x 8 + 1

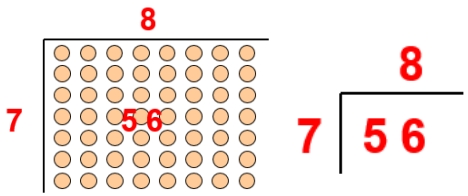
Division at Ravensbury

Year 4	Year 5	Year 6
÷ = signs and missing numbers Continue using a range of equations as in year 3 but with appropriate numbers. **Sharing, Grouping and using a number line** Children will continue to explore division as sharing and grouping, and to represent calculations on a number line until they have a secure understanding. Children should progress in their use of written division calculations: • Using tables facts with which they are fluent • Experiencing a logical progression in the numbers they use, for example: 1. Dividend just over 10x the divisor, e.g. 84 ÷ 7 2. Dividend just over 10x the divisor when the divisor is a teen number, e.g. 173 ÷ 15 (learning sensible strategies for calculations such as 102 ÷ 17) 3. Dividend over 100x the divisor, e.g. 840 ÷ 7 4. Dividend over 20x the divisor, e.g. 168 ÷ 7 All of the above stages should include calculations with remainders as well as without. Remainders should be interpreted according to the context. (I.e. rounded up or down to relate to the answer to the problem) **e.g. 840 ÷ 7 = 120** *Jottings* *7 x 100 = 700* *7 x 10 = 70* *7 x 20 = 140*  		**÷ = signs and missing numbers** **Continue using a range of equations but with appropriate numbers** **Sharing and Grouping and using a number line** **Children will continue to explore division as sharing and grouping, and to represent calculations on a number line as appropriate.** **Quotients should be expressed as decimals and fractions** **Formal Written Methods – long and short division** **E.g. 1504 ÷ 8**
Formal Written Methods Formal short division should only be introduced once children have a good understanding of division, its links with multiplication and the idea of 'chunking up' to find a target number (see use of number lines above) Short division to be modelled for understanding using place value counters as shown below. Calculations with 2 and 3-digit dividends.	**Formal Written Methods** Continued as shown in Year 4, leading to the efficient use of a formal method. The language of grouping to be used (see link from fig. 1 in Year 4) E.g. 1435 ÷ 6	



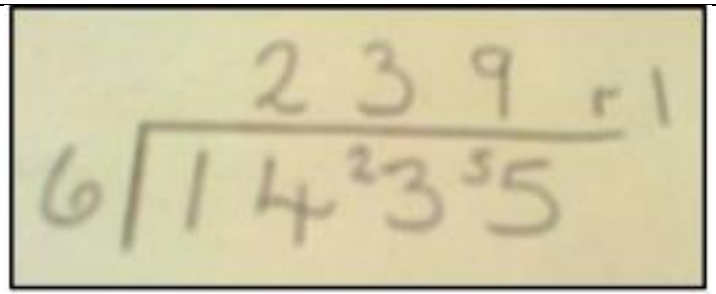
Mental Methods
Children should experience regular counting on and back from different numbers in multiples of 6, 7, 9, 25 and 1000.
Children should learn the multiplication facts to 12 x 12.

Towards a formal written method
Alongside pictorial representations and the use of models and images, children should progress onto short division using a bus stop method.



Place value counters can be used to support children apply their knowledge of grouping. Reference should be made to the value of each digit in the dividend.

Each digit as a multiple of the divisor
'How many groups of 3 are there in the hundreds column?'
'How many groups of 3 are there in the tens column?'
'How many groups of 3 are there in the units/ones

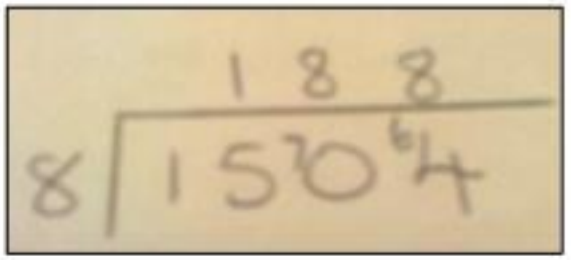


Children begin to practically develop their understanding of how express the remainder as a decimal or a fraction. Ensure practical understanding allows children to work through this (e.g. what could I do with this remaining 1? How could I share this between 6 as well?)

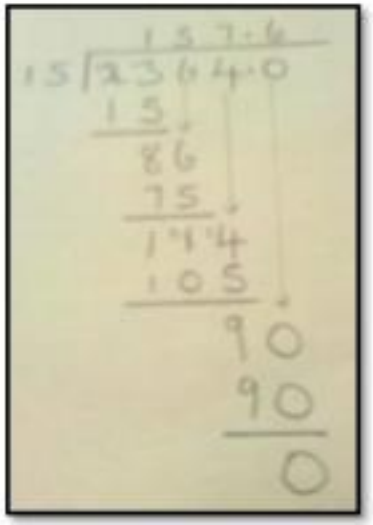
Mental Methods
Children should count regularly using a range of multiples, and powers of 10, 100 and 1000, building fluency.
Children should practice and apply the multiplication facts to 12 x 12.

Vocabulary
common factors
prime number, prime factors
composite numbers
short division
square number
cube number
inverse
power of
see year 4

Questions for Mastery and Reasoning
The = sign means equality. Take it in turn to change one side of this equation, using multiplication and division, e.g.
Start: **24 = 24**
Player 1: **4 x 6 = 24**
Player 2: **4 x 6 = 12 x 2**
Player 1: **48 ÷ 2 = 12 x 2**



E.g. 2364 ÷ 15



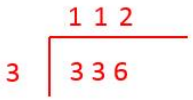
Mental Strategies
Children should count regularly, building on previous work in previous years.
Children should practice and apply the multiplication facts to 12 x 12.

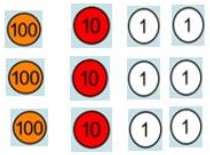
Vocabulary
see years 4 and 5

Questions for Mastery and Reasoning

Sometimes, always, never true questions about multiples and divisibility. E.g.: If a number is divisible by 3 and 4, it will also be divisible by 12.

column?'





When children have conceptual understanding and fluency using the bus stop method without remainders, they can then progress onto 'carrying' their remainder across to the next digit.

Questions for Mastery and Reasoning

True or false? Dividing by 10 is the same as dividing by 2 and then dividing by 5. Can you find any more rules like this?

Is it sometimes, always or never true that □ ÷ Δ = Δ ÷ □?

Inverses and deriving facts. 'Know one, get lots free!' e.g.: 2 x 3 = 6, so 3 x 2 = 6, 6 ÷ 2 = 3, 60 ÷ 20 = 3, 600 ÷ 3 = 200 etc.

Sometimes, always, never true questions about multiples and divisibility. (When looking at the examples on this page, remember that they **may not** be 'always true'!) E.g.:

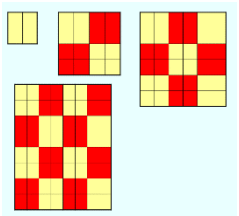
- Multiples of 5 end in 0 or 5.
- The digital root of a multiple of 3 will be 3, 6 or 9.
- The sum of 4 even numbers is divisible by 4.

Vocabulary

divide, divided by, divisible by, divided into
share between, groups of
factor, factor pair, multiple

Sometimes, always, never true questions about multiples and divisibility. E.g.:

- If the last two digits of a number are divisible by 4, the number will be divisible by 4.
- If the digital root of a number is 9, the number will be divisible by 9.
- When you square an even number the result will be divisible by 4 (one example of 'proof' shown left)



Using what you know about rules of divisibility, do you think 7919 is a prime number? Explain your answer.

times as (big, long, wide …etc.) equals, remainder, quotient, divisor inverse *see years 1-3*		